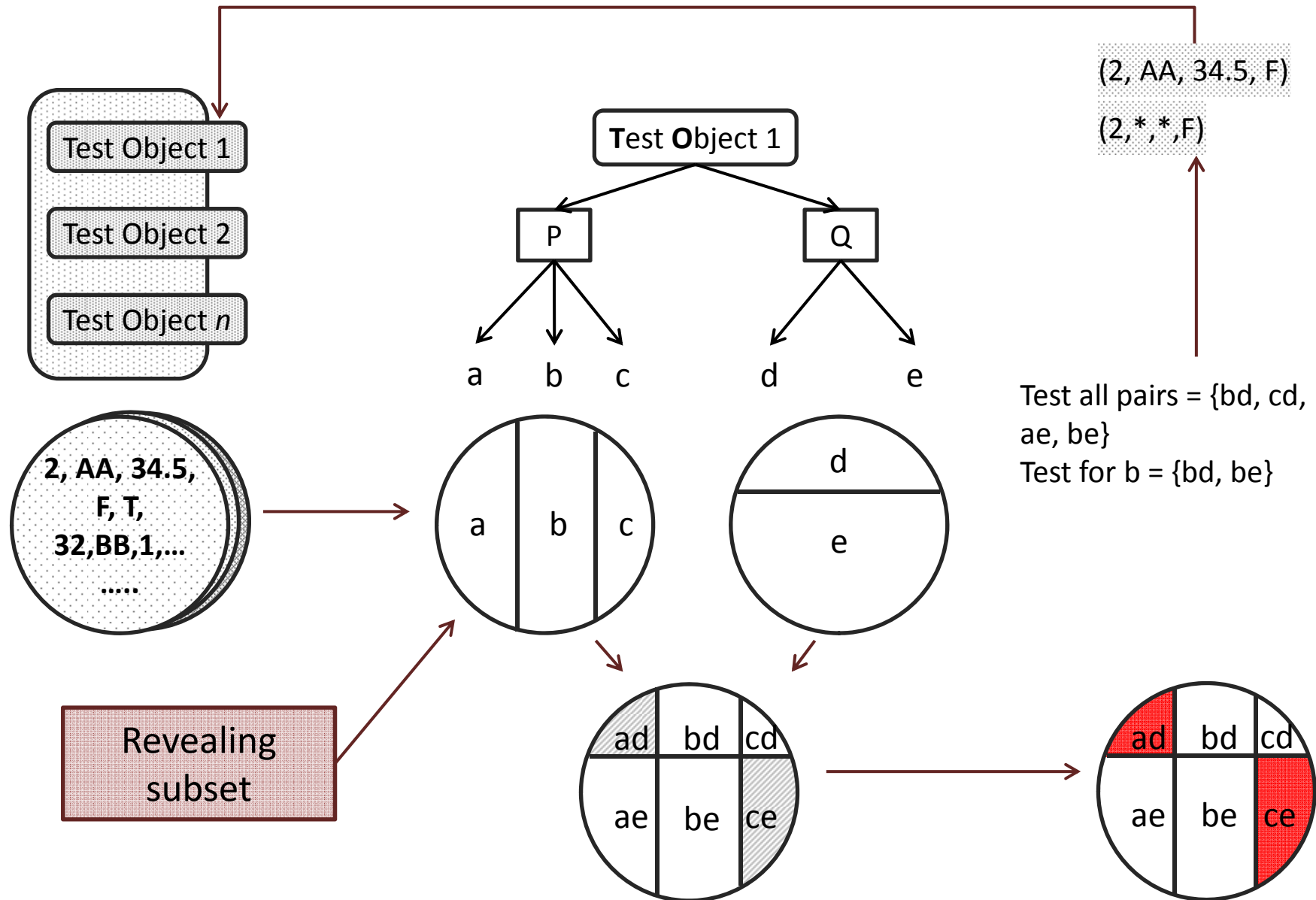


Integrating the classification tree method with combinatorial testing: test selection strategy

Eduardo Miranda, PhD.
CMU/MSE
MSE/NIST Seminar
June 7th, 2011
Pittsburgh, PA

The Classification Tree Method illustrated



Partition and boundary value analysis

- Two types of faults:
 - Computation faults: The wrong function is applied to some subdomain S_i in the implementation
 - Domain faults: The boundary between two subdomains S_i, S_j in the implementation is wrong
- Partition testing
 - Test inputs are designed to find computation faults
- Boundary value analysis
 - BVA aims to find domain faults by using test inputs near the boundaries

How do we build confidence that a subset is revealing?

- If it is possible to establish an order relationship on the members of a given subset we can use boundary value analysis
 - Quantities
 - Lengths
 - Collection of elements
 - Positions
 - Distance
- Test catalogues
- Unless the subset has only one member, the absolute minimum number of values to test is 2

Simple test catalog

Boolean

[in/out] True

[in/out] False

Enumeration

[in/out] Each enumerated value

[in] Some value outside the enumerated set

Range $L \dots U$

[in] $L - 1$ (the element immediately preceding the lower bound)

[in/out] L (the lower bound)

[in/out] A value between L and U

[in/out] U (the upper bound)

[in] $U + 1$ (the element immediately following the upper bound)

Numeric Constant C

[in/out] C (the constant value)

[in] $C - 1$ (the element immediately preceding the constant value)

[in] $C + 1$ (the element immediately following the constant value)

[in] Any other constant compatible with C

Non-Numeric Constant C

[in/out] C (the constant value)

[in] Any other constant compatible with C

[in] Some other compatible value

Sequence

[in/out] Empty

[in/out] A single element

[in/out] More than one element

[in/out] Maximum length (if bounded) or very long

[in] Longer than maximum length (if bounded)

[in] Incorrectly terminated

Scan with action on elements P

[in] P occurs at beginning of sequence

[in] P occurs in interior of sequence

[in] P occurs at end of sequence

[in] PP occurs contiguously

[in] P does not occur in sequence

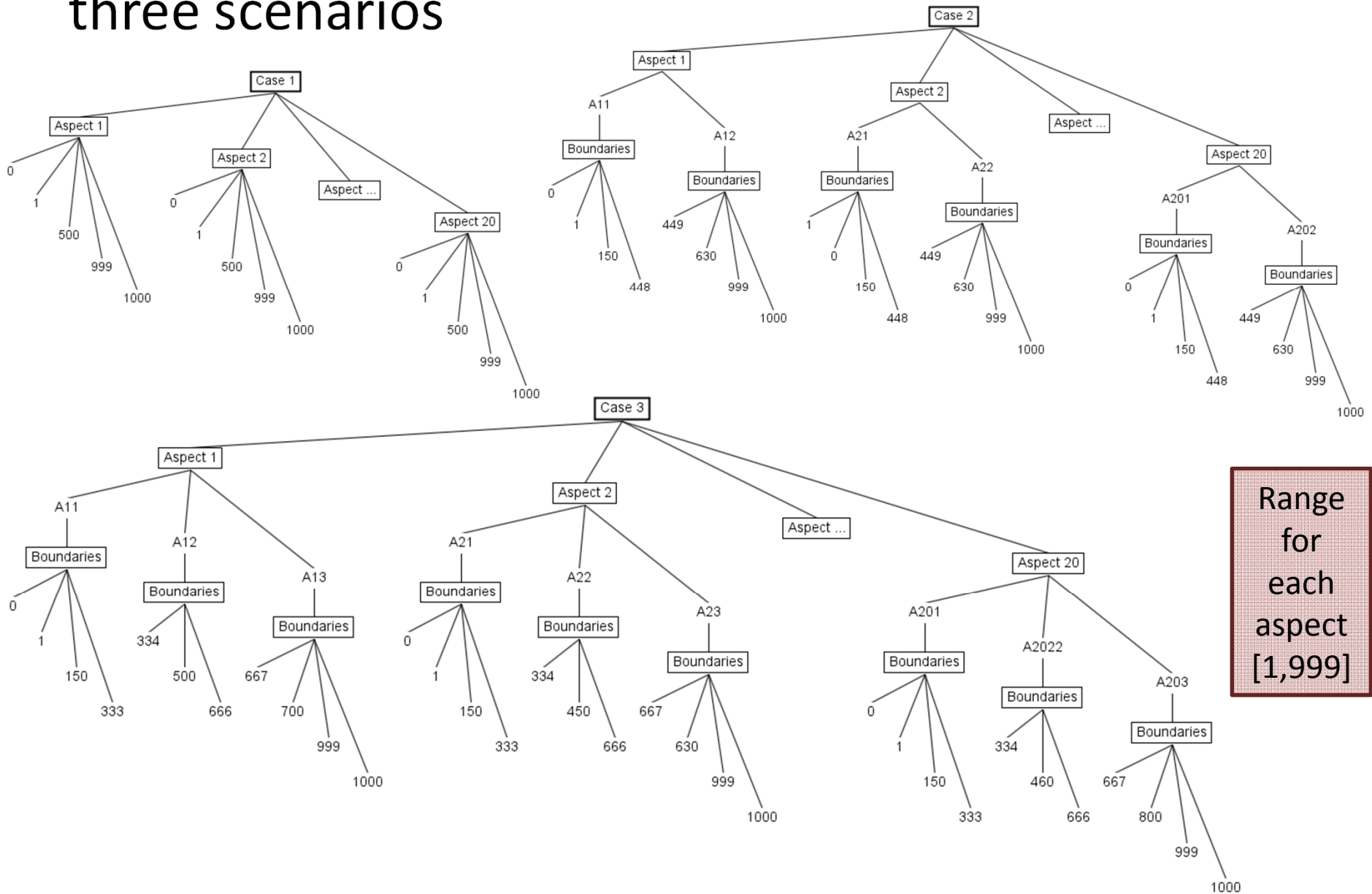
[in] pP where p is a proper prefix of P

[in] Proper prefix p occurs at end of sequence

At what level should we employ interaction testing?

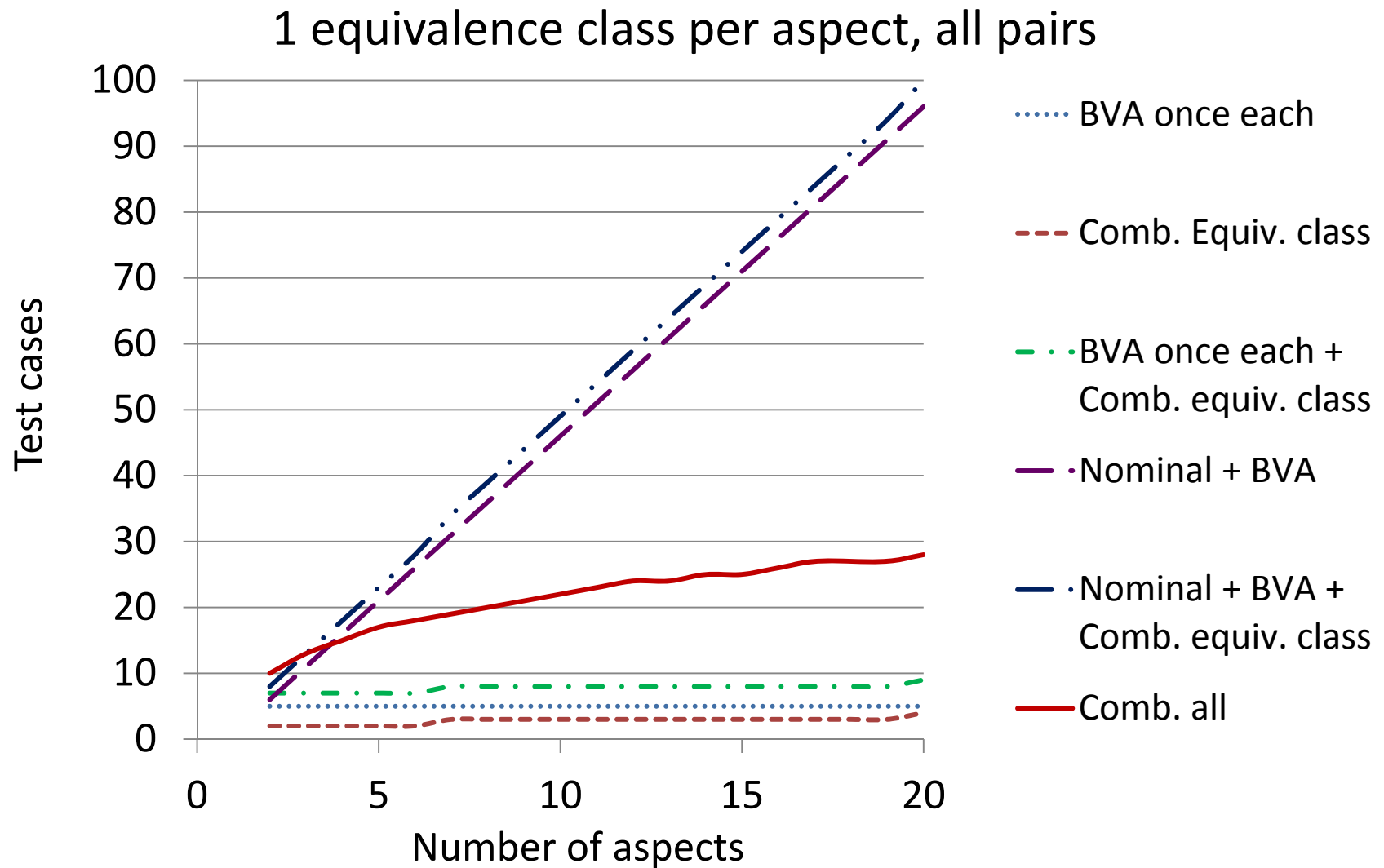
- If we are using BVA to establish confidence in a subdomain:
 - Should we use the BVA values (left-, left, middle, right, right +) in the interactions?
 - Should we first establish confidence on the equivalence class and then test for interactions?
 - What happens if we are not using BVA?
- What do we do with invalid values?

To answer the previous questions we will look at three scenarios



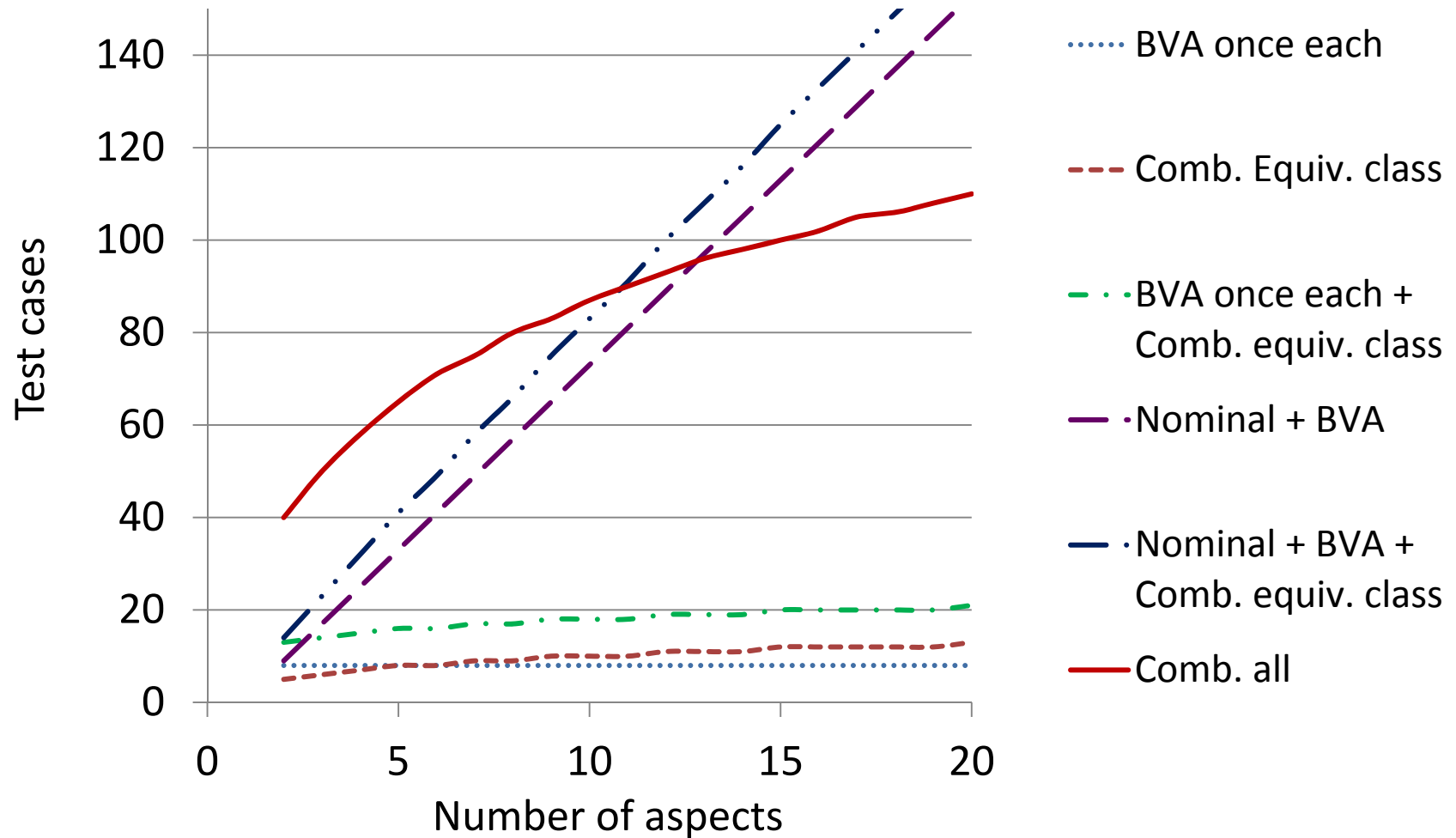
Range for each aspect [1,999]

Number of test cases required by different strategies (1)

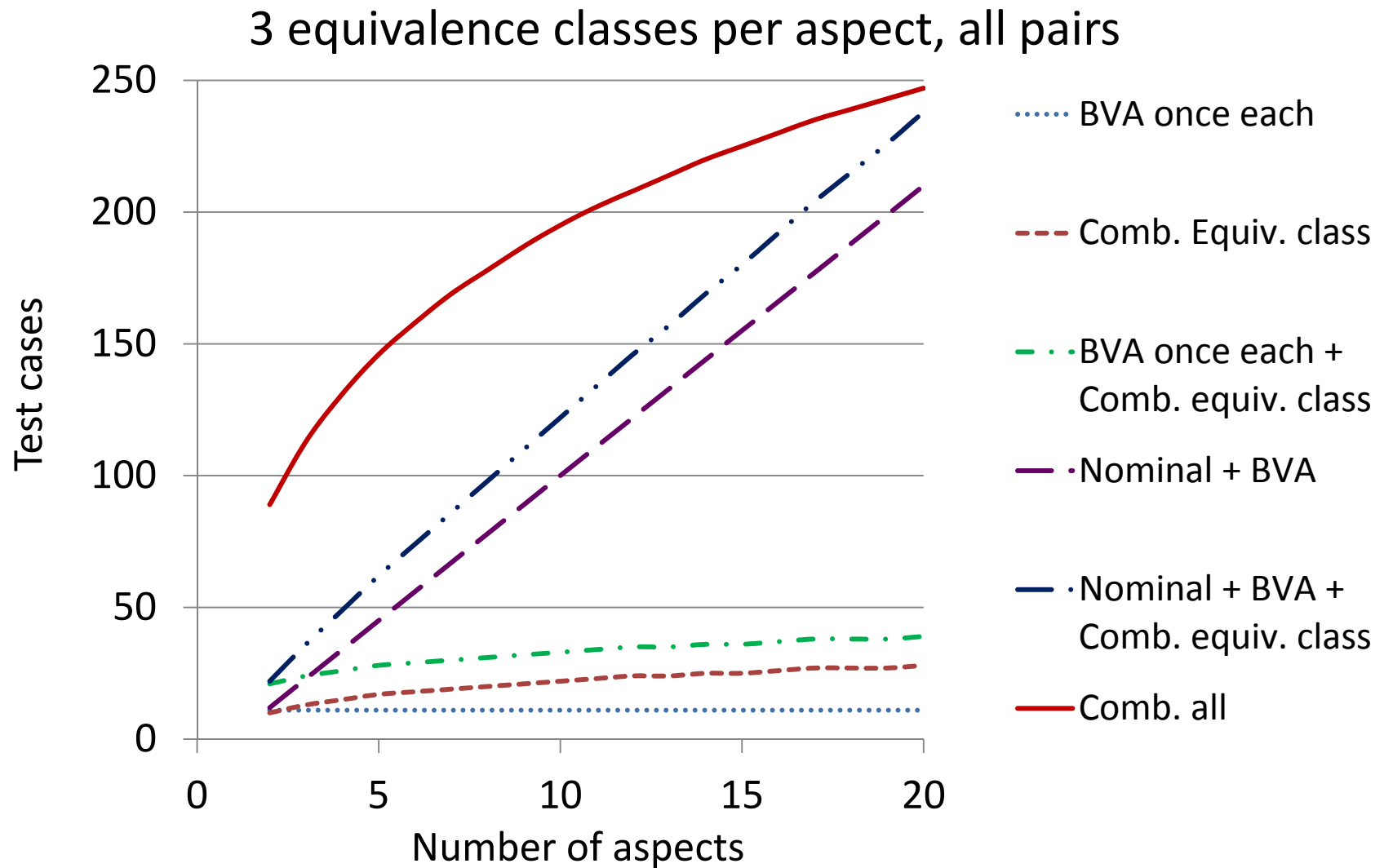


Number of test cases required by different strategies (2)

2 equivalence classes per aspect, all pairs



Number of test cases required by different strategies (3)



Comparison of different strategies on the basis of fault finding effectiveness (1)


intended behavior

1. X = "Don't know"
2. if T then
 1. if $1 \leq V \leq 99$ then
 1. x = "V1"
 2. endif
3. else
 1. If $100 \leq V \leq 200$ then
 1. x = "V2"
 2. endif
4. endif
5. print (x)

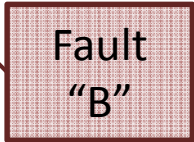
programmed behavior

1. X = "Don't know"
2. if T then
 1. if $1 \leq V < 99$ then
 1. x = "V1"
 2. endif
3. else
 1. If $100 \leq V < 200$ then
 1. x = "V2"
 2. endif
4. endif
5. print (x)

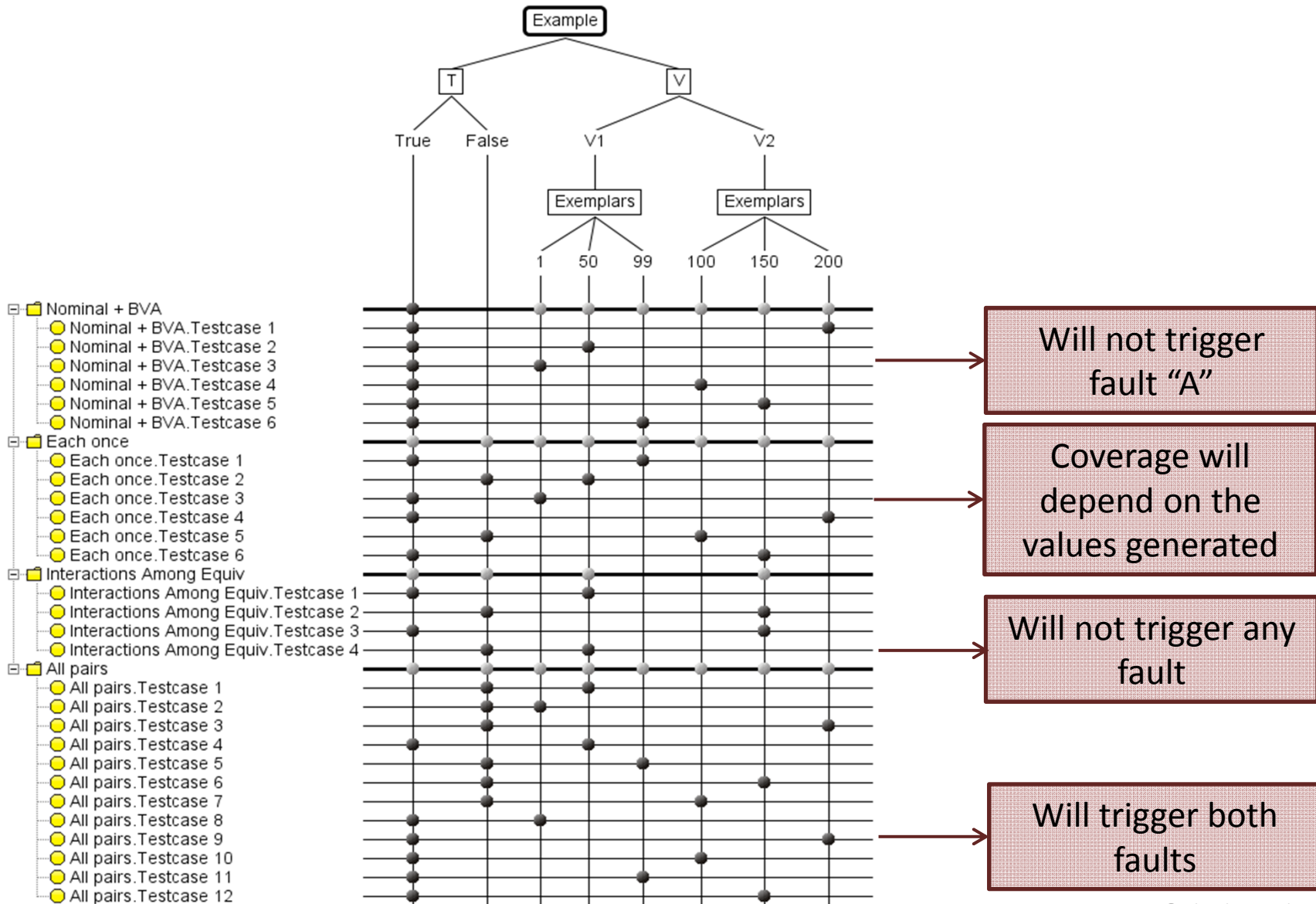
Fault
"A"



Fault
"B"



Comparison of different strategies on the basis of fault finding effectiveness (2)



What about negative testing

- Should we mix positive and negative testing?
- Should we test for combinations of invalid values or it suffices with all singles testing?

Fault masking

All pairs array

| | V | U | Z |
|----|---------|---|----|
| 1 | V1 | 1 | Z1 |
| 2 | V2 | 2 | Z1 |
| 3 | V3 | 3 | Z1 |
| 4 | Invalid | 4 | Z1 |
| 5 | V1 | 2 | Z2 |
| 6 | V2 | 1 | Z2 |
| 7 | V3 | 4 | Z2 |
| 8 | Invalid | 3 | Z2 |
| 9 | V1 | 3 | Z3 |
| 10 | V2 | 4 | Z3 |
| 11 | V3 | 1 | Z3 |
| 12 | Invalid | 2 | Z3 |
| 13 | V1 | 4 | Z4 |
| 14 | V2 | 3 | Z4 |
| 15 | V3 | 2 | Z4 |
| 16 | Invalid | 1 | Z4 |
| 17 | V1 | 1 | Z5 |
| 18 | V2 | 2 | Z5 |
| 19 | V3 | 3 | Z5 |
| 20 | Invalid | 4 | Z5 |

The fault is masked by the invalid value in row 4

```
if V = "Invalid" then  
    display message  
    exit  
endif
```

```
.  
.   
if z = z1 then  
     $x := 6 / (u - 4)$   
endif
```

Exercising invalid combinations

Is V1 = invalid, V2 = invalid and V3 = invalid a good test case?

```
if V1 is invalid then  
    display Error1  
    exit  
endif  
if V2 is invalid then  
    display Error2  
    exit  
endif  
If V3 is invalid then  
    display Error3  
    exit  
endif
```

```
if V1 is invalid then  
    V1 = DefaultValue1  
endif  
if V2 is invalid then  
    V2 = DefaultValue2  
endif  
if V3 is invalid then  
    V3 = DefaultValue3  
endif
```

Summary

- In testing you get what you pay for. Do not compare the cost of a method to the cost of not testing, because the latter will always require less test cases
- Combinatorial testing
 - Very good and efficient at finding computational faults
 - Very good, but expensive at finding domain problems. Still, what would be a better approach is an open issue
- Unless there is a fault model conjecture for doing something else:
 - Keep negative testing separate from positive one
 - Don not combine invalid values
- To verify equivalence within a class
 - Combinations might act as confounders
 - For 1 or 2 equivalence classes within each aspect, combinatorial testing is feasible and effective. For three or more, the number of test cases required becomes very large and all singles might be a good alternative
 - One at a time testing will eliminate confounding but interactions might mask faults and will require a large number of test cases

Questions?